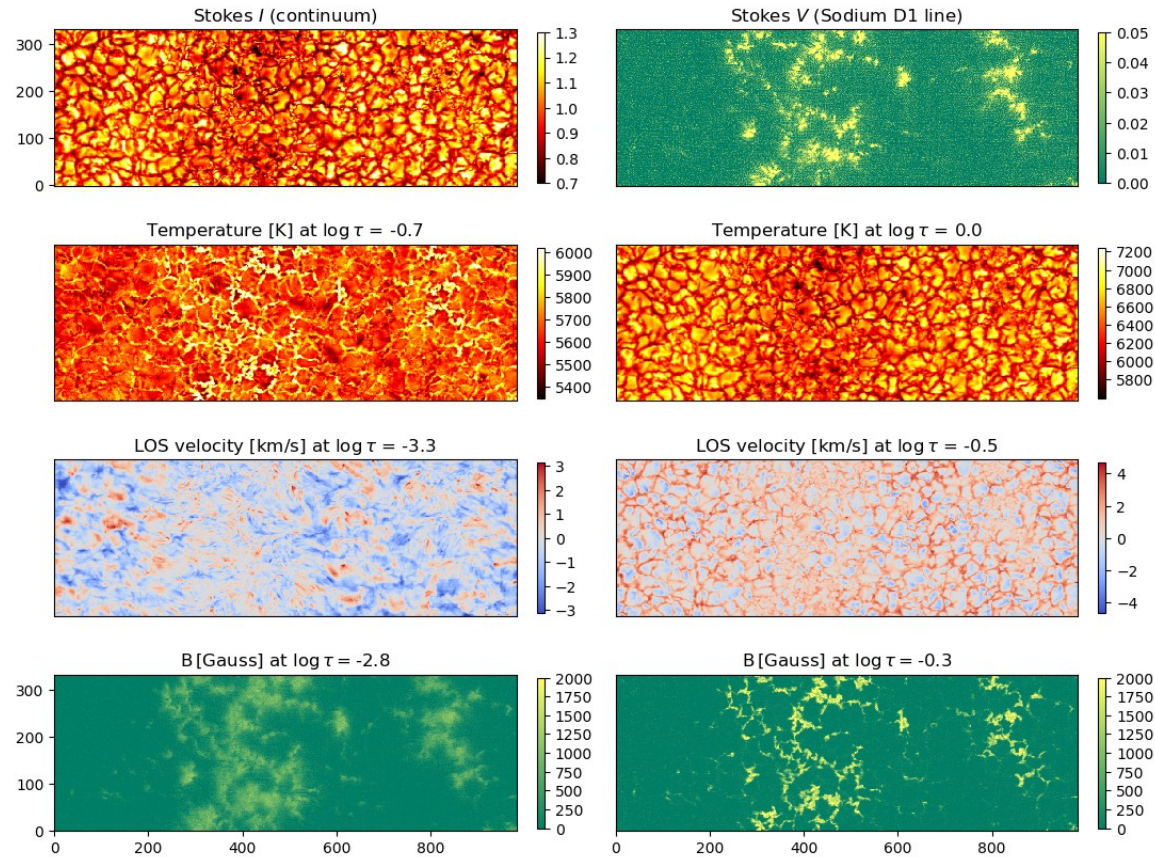


Comparing inversion strategies for  
active region photospheres

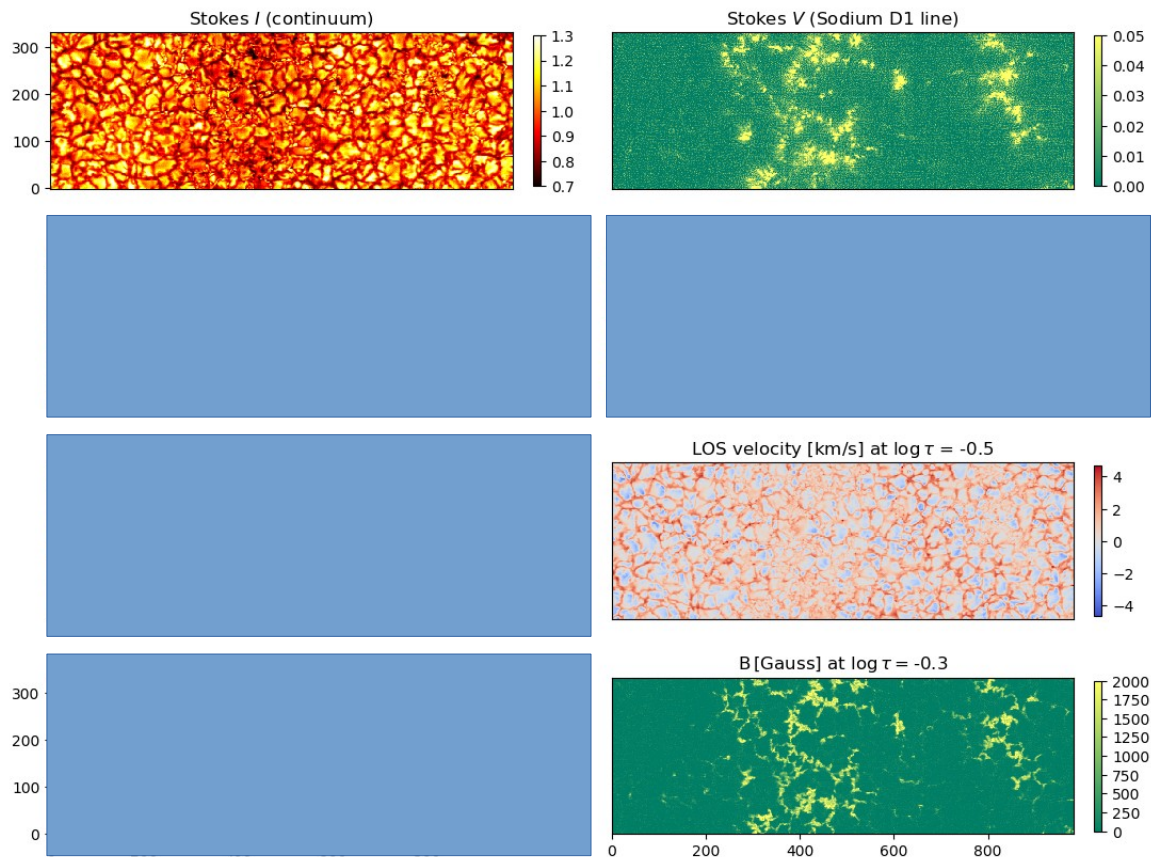
# Brief reminder on the inversions

- Methods that fit a depth-dependent atmospheric model to the observed Stokes spectrum.
- Applying them pixel by pixel we get a 2D map or a pseudo-3D model of the observed region
- Several degrees of physical assumptions → we have to choose according to the complexity and according to our data.
- Let's describe them quickly



# Milne-Eddington inversions

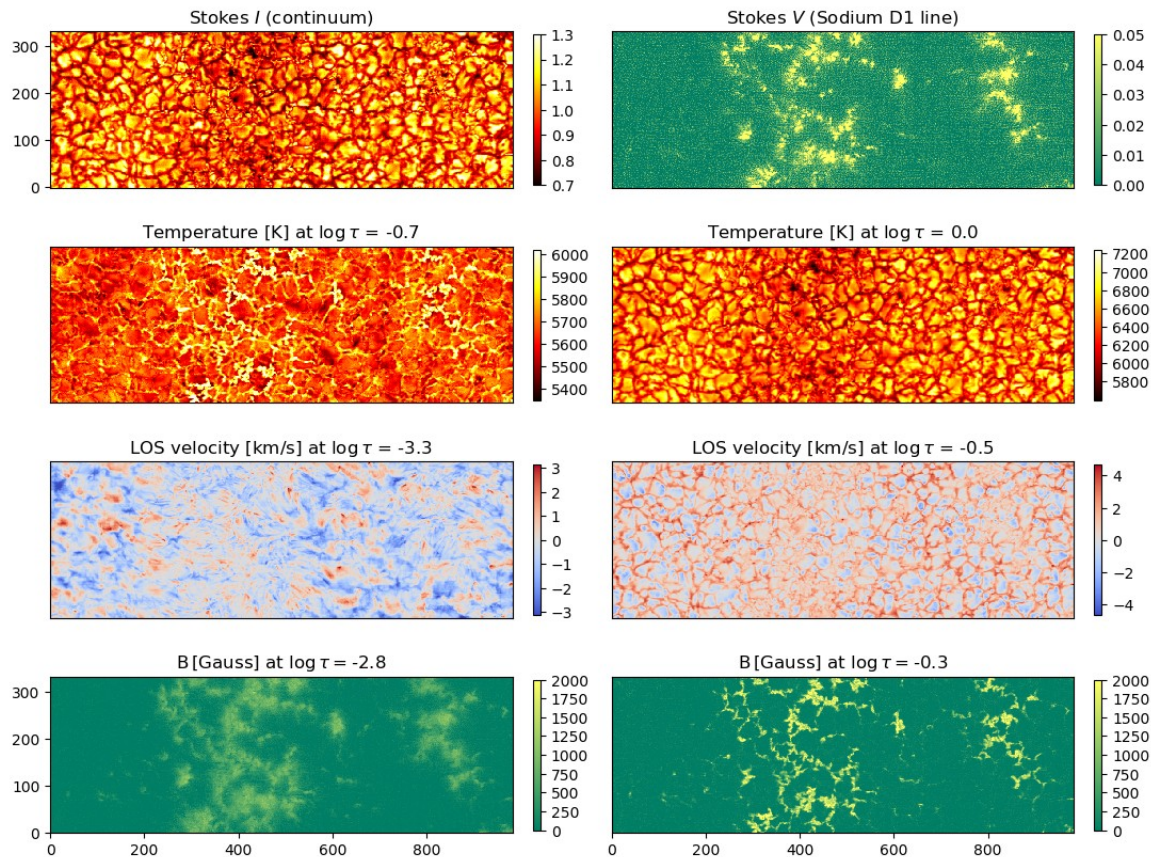
- All physical parameters are considered constants, except for the source function that has a slope in order to reproduce line depth
- Only meaningful information is the magnetic field vector and the line-of-sight velocity
- Can't be applied to multi-line observations (unless the lines are very similar).
- Incredibly fast: ms per pixel, easy to implement spatial coupling (will be important later).





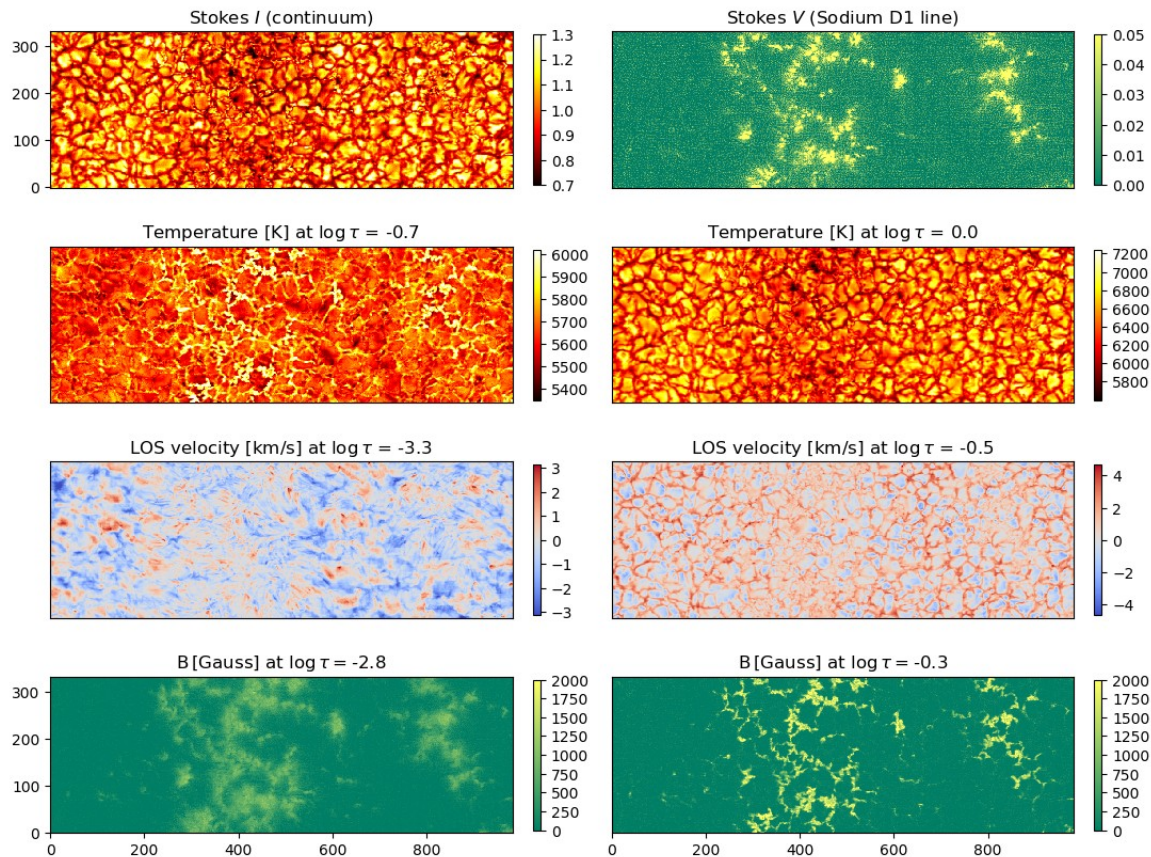
# LTE (SIR) inversions

- Consider a depth dependent atmosphere where the RTE solution is numerical and opacity and emissivity follow from the Saha and Boltzman equations
- It's possible to capture depth dependence of temperature, velocity magnetic field...
- Can be applied to photospheric lines (even chromospheric with some ad-hoc corrections)
- Fast: seconds per pixel. (To get runtime @ a 256 node server, for a 1000 x 1000 map, replace seconds with hours).



# NLTE (StIC) inversions

- Consider a depth dependent atmosphere where the RTE solution is numerical and opacity and emissivity **don't** follow from the Saha and Boltzman equations
- Can be self-consistently applied to chromospheric lines
- Not so fast: minutes per pixel (can be major hassle to execute them).
- The only way to self-consistently interpret Sodium D lines, Ca II 8542, Mg I b2... etc.

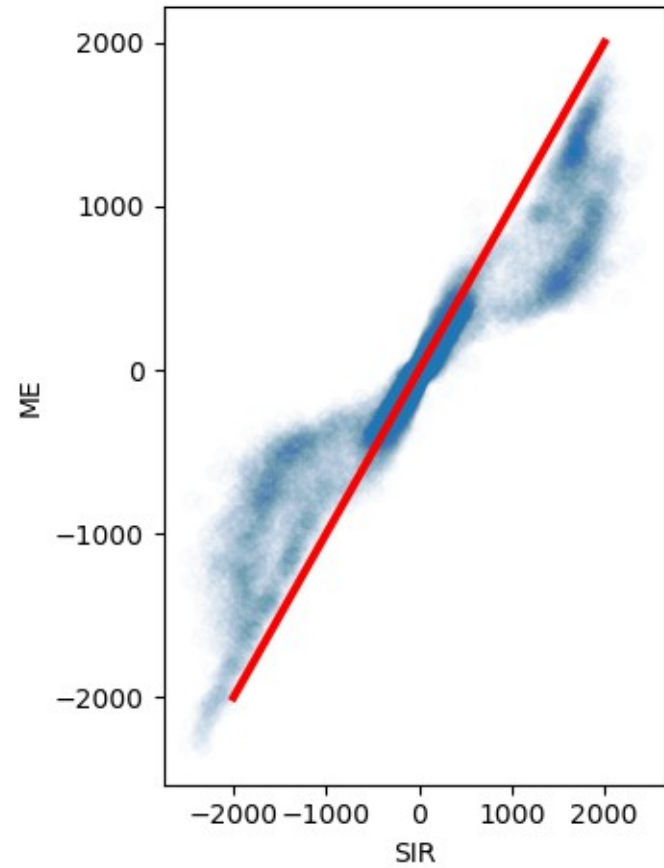
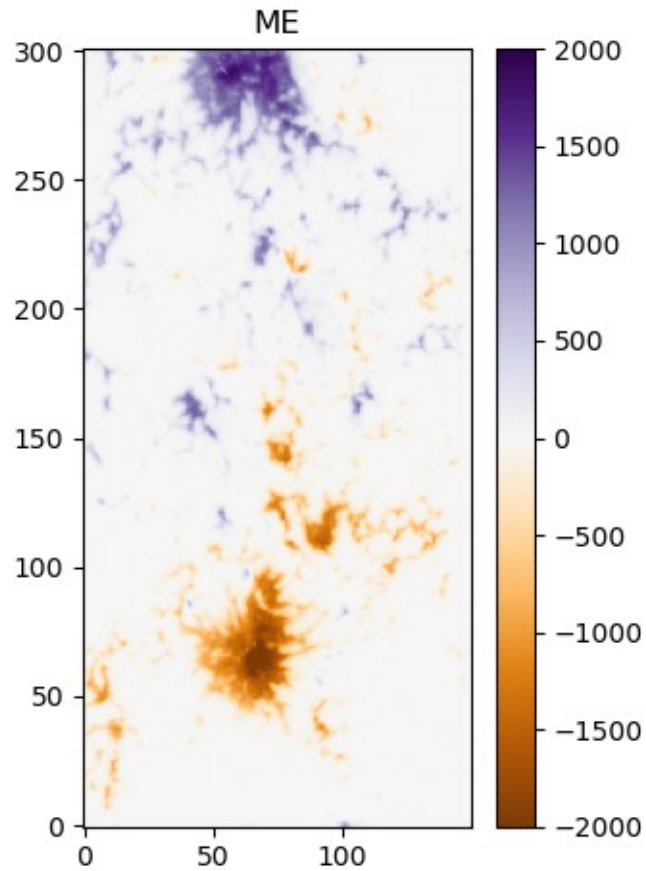
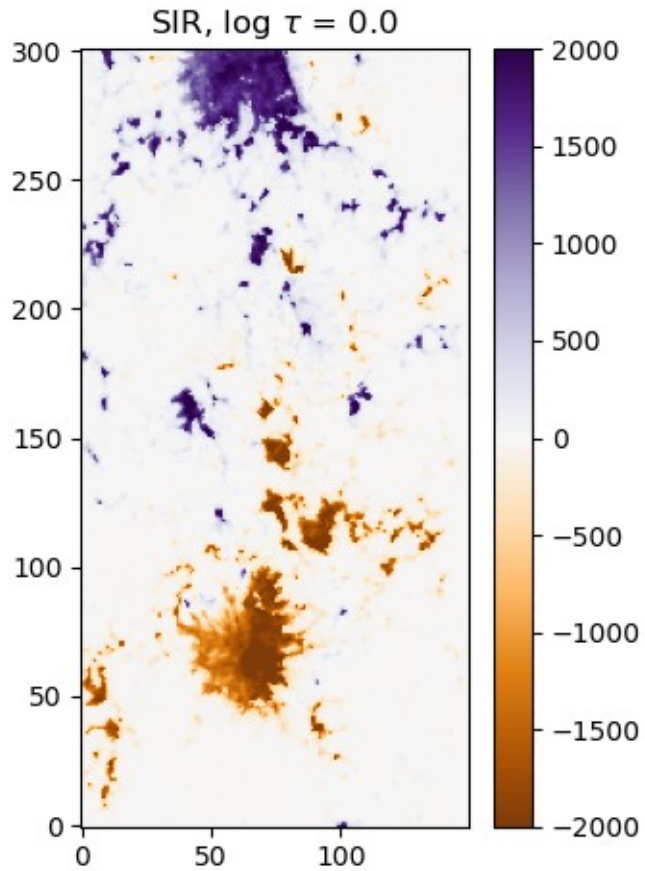


# Here we are comparing ME inversion and SIR

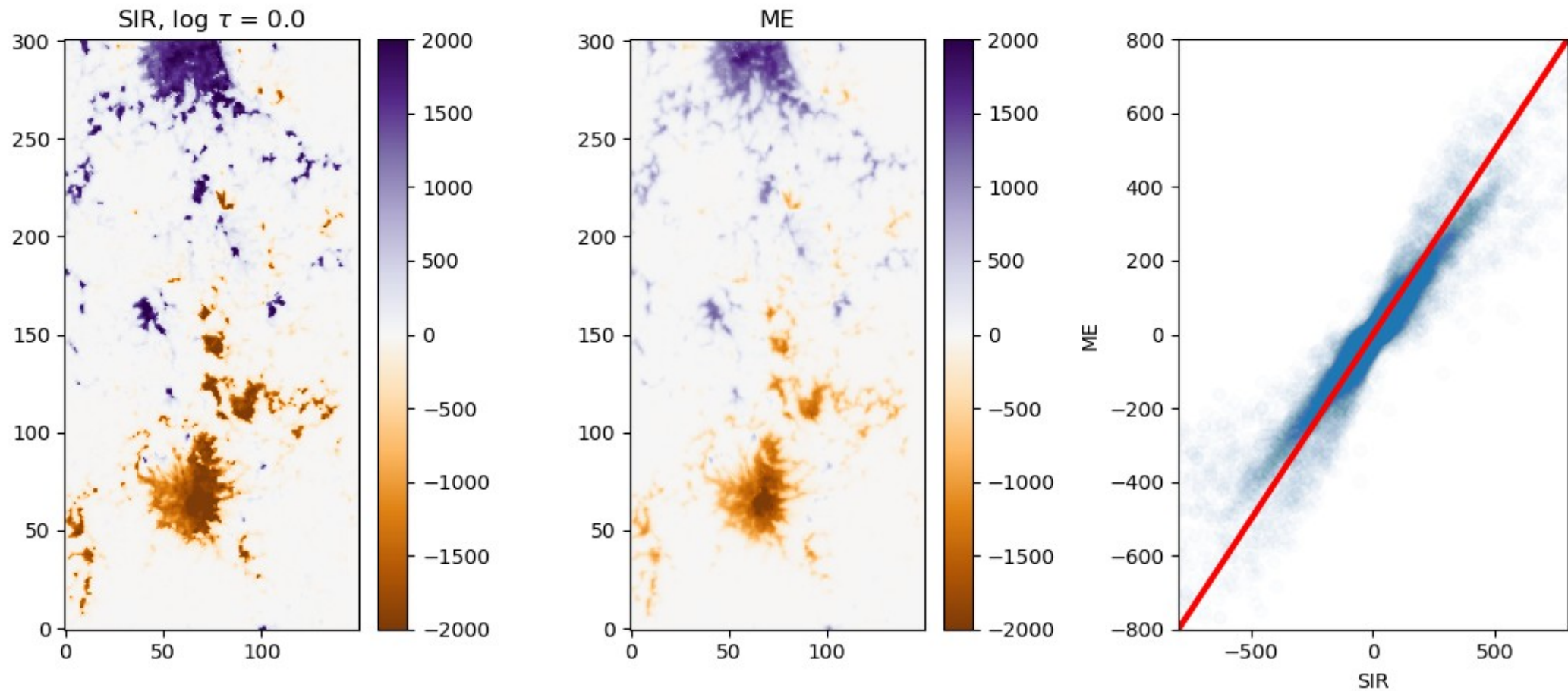
- The motivation came from an “S” shape that we saw in some comparisons between Na D inversions and extrapolations from the photosphere at the last ISSI meeting (in spring)
- A usual suspect is the inversion method: because of the noise, poor sensitivity or too complex model, weird variations in the physical parameters can appear.
- The test: compare Milne-Eddington inversion (everything constant), and a SIR inversion (in this case, linear gradient of the magnetic field) with each other.
- Data: Hinode active region observed at 30/09/2018 – two photospheric neutral Iron lines
- Keep mind that ME gives 1 value, while SIR gives a **depth dependent magnetic field**
- Range of sensitivities of the Fe I lines is from  $\log \tau = 0$  to  $\log \tau = -2$ , on average.
- This translates to a  $\sim 300$  km height span.



# ME vs SIR at deep photosphere

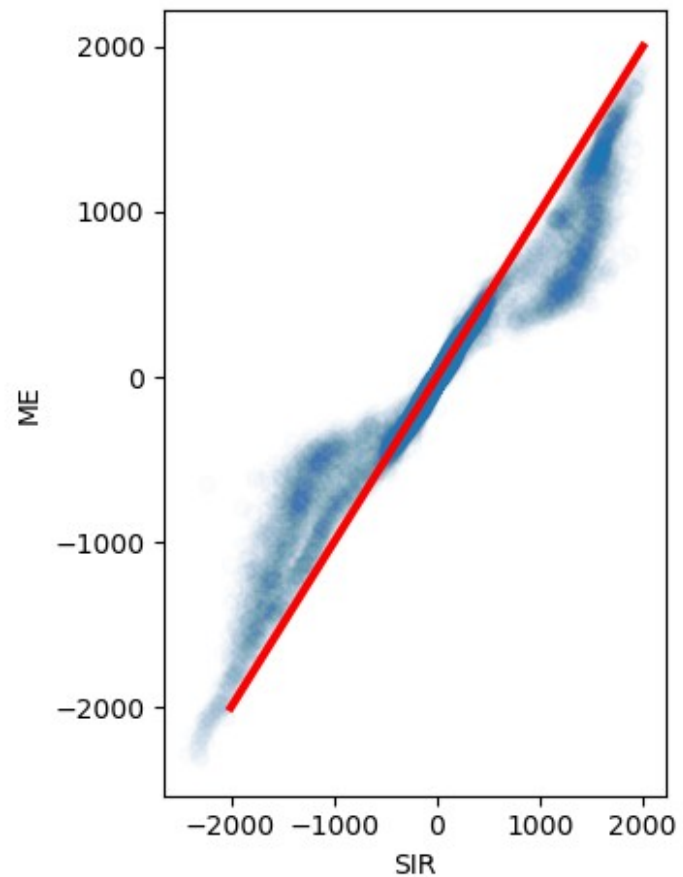
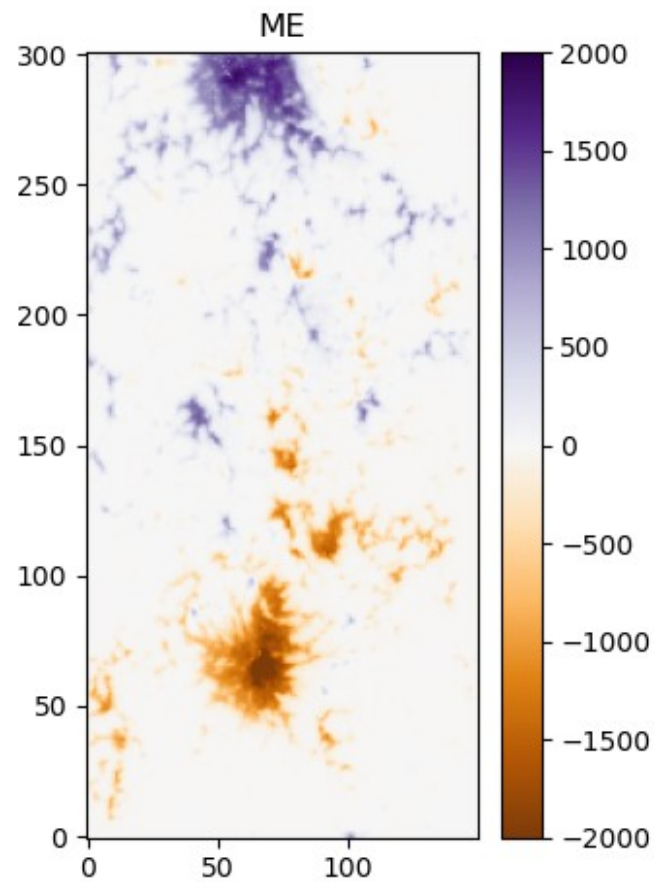
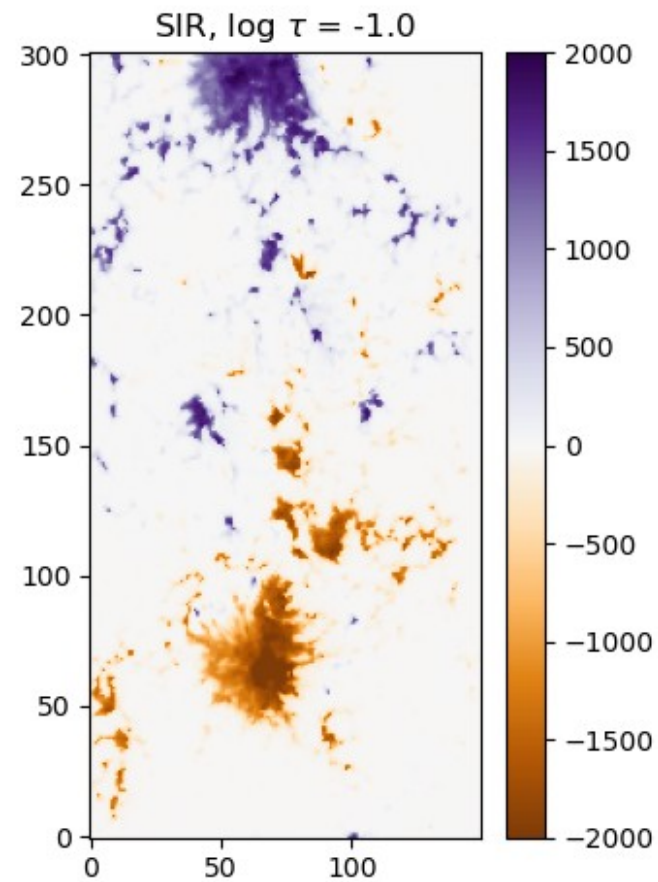


# ME vs SIR at deep photosphere – weak fields

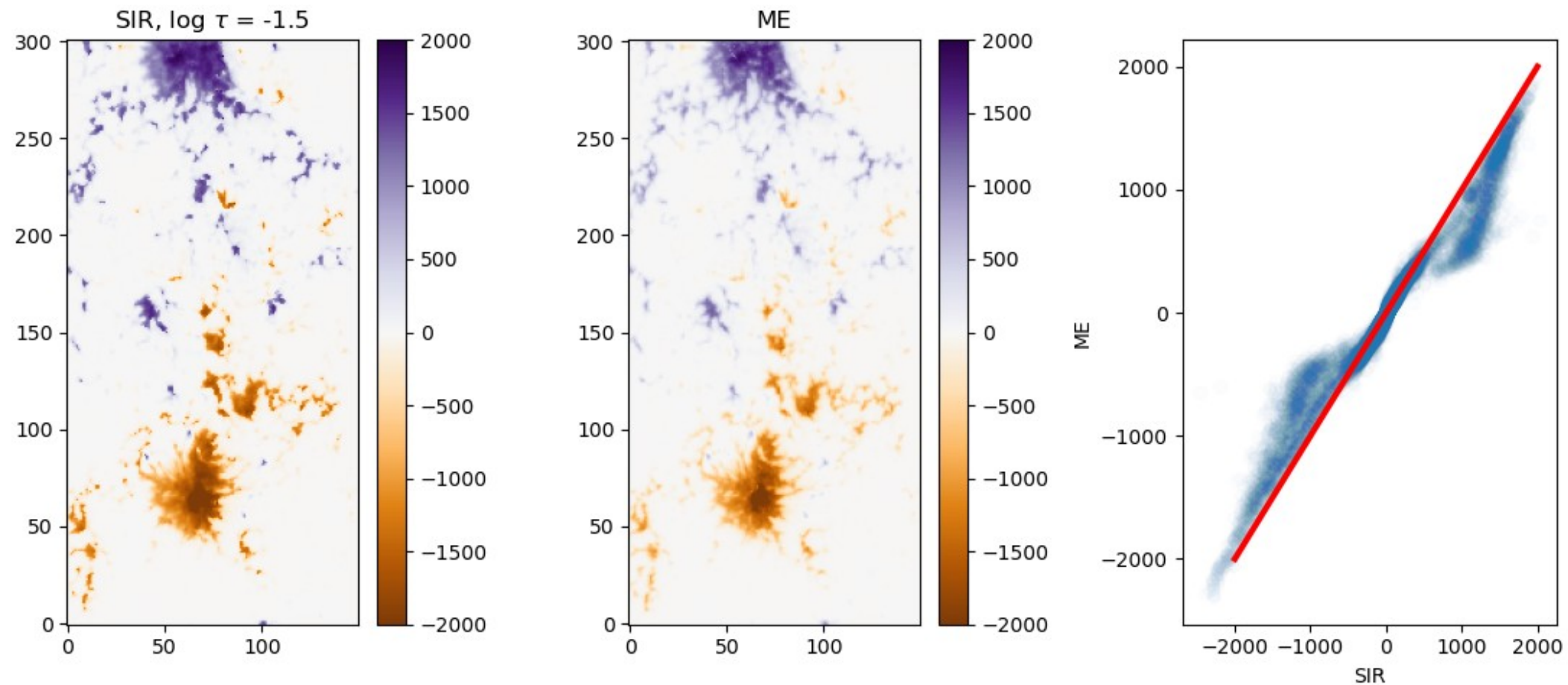




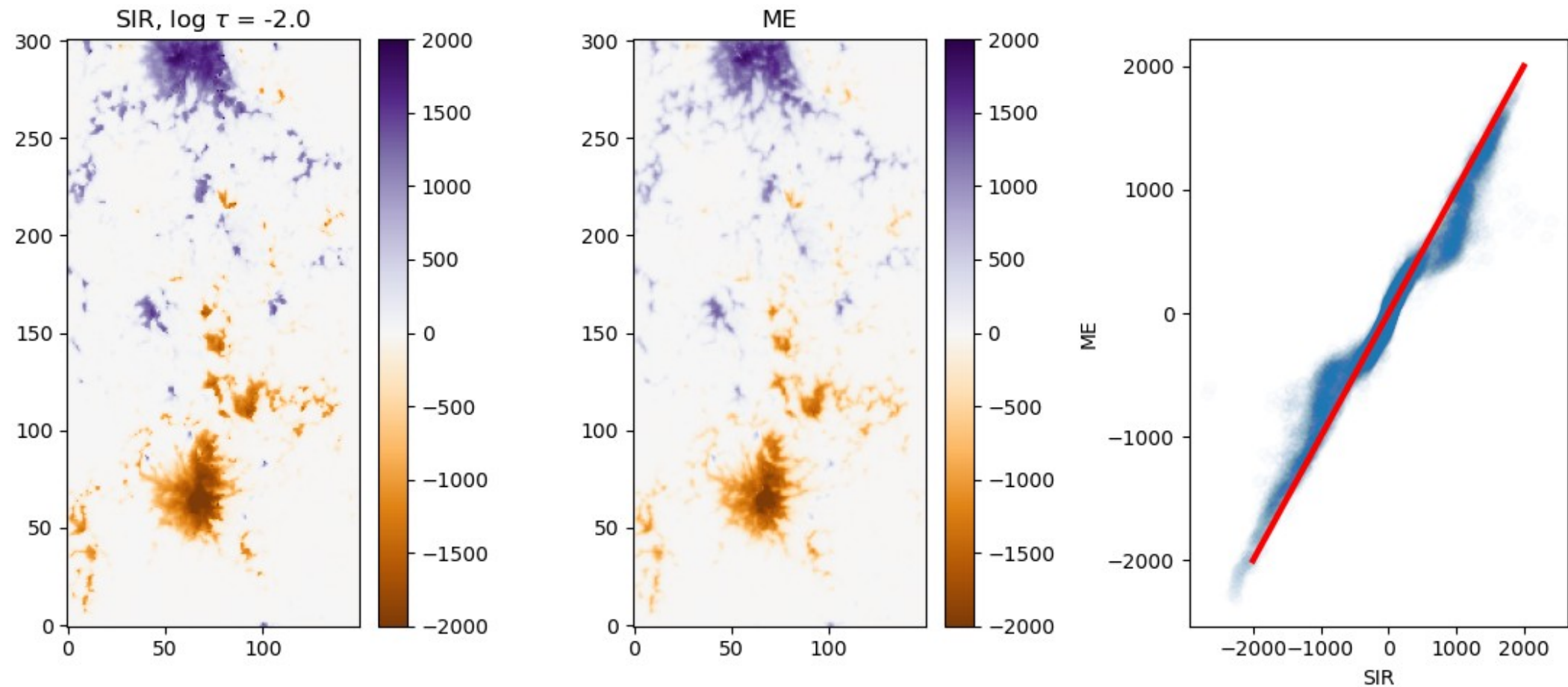
# ME vs SIR comparison at $\log \tau = -1.0$



# ME vs SIR at peak sensitivity of Fe I ( $\log \tau = -1.5$ )



# ME vs SIR at upper photosphere ( $\log \tau = -2$ )



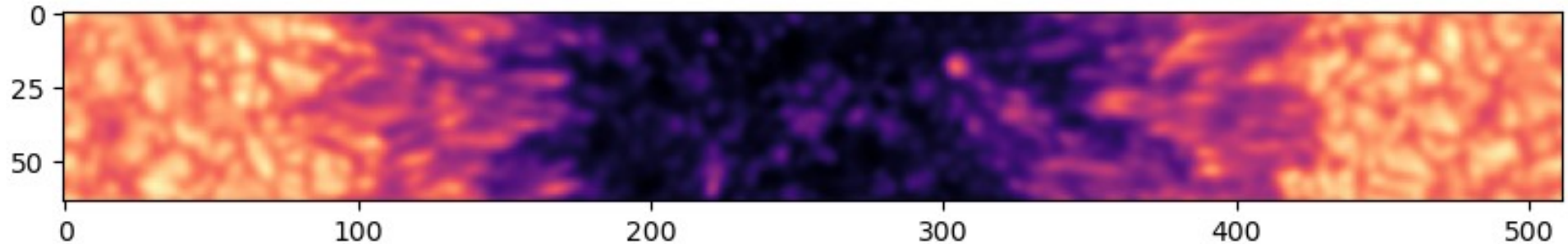


# Why is this so?

- My initial suspicion was that this is due to intricacies in the line formation
- Different atmospheres have different structures and different **response functions**
- ME atmosphere infers some mean magnetic field over the line formation region and it will be equal to the actual B at different depths in different features (umbra, penumbra, QS...)
- How to check that?
- Come in with the known solution, i.e. simulation

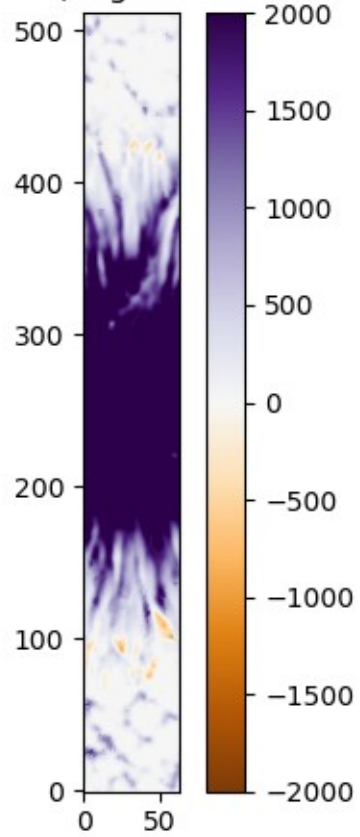
# Double-checking on simulated data

- Slice of the Sunspot simulation, used in Borrero et al. (2019), provided by M. Rempel, 16 km horizontal 12 km vertical resolution.
- Synthesize the Hinode lines using SIR
- Apply spectral and spatial degradation, to make it look like Hinode SOT/SP data
- Invert using M-E and SIR, and compare
- Below: Continuum intensity from the simulated dataset. Note much much smaller FoV.

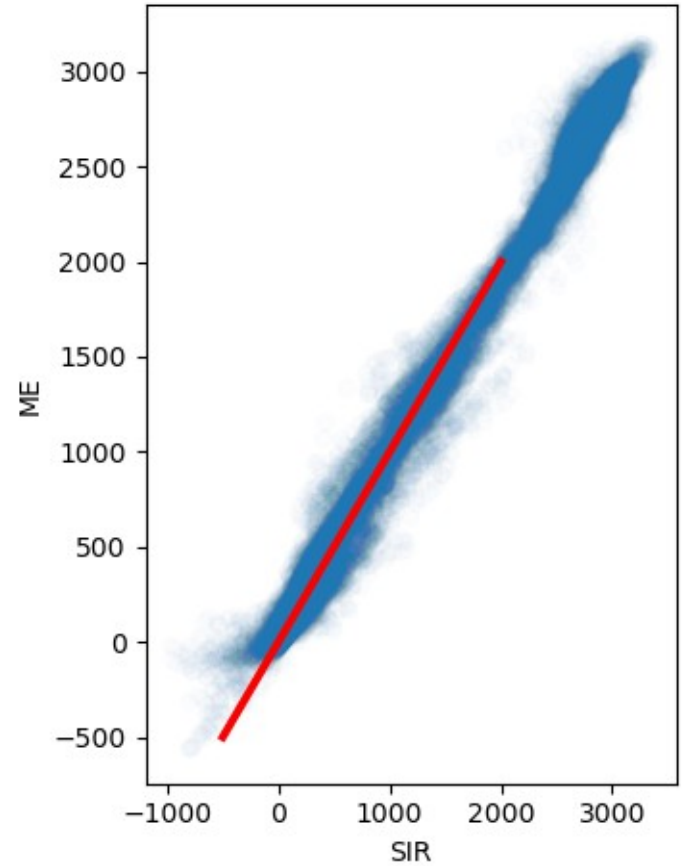
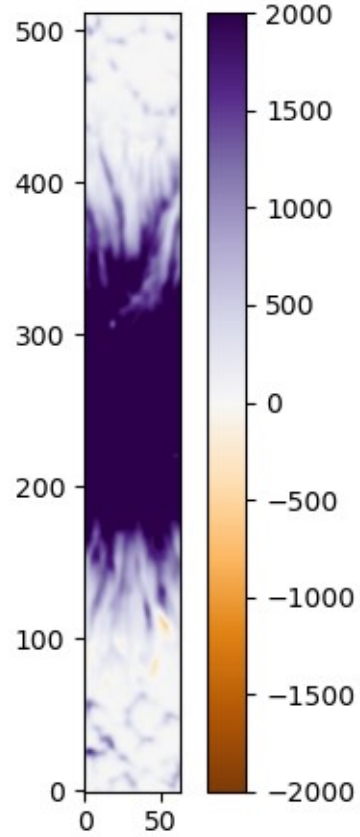


# ME vs SIR at deep photosphere

SIR,  $\log \tau = 0.0$

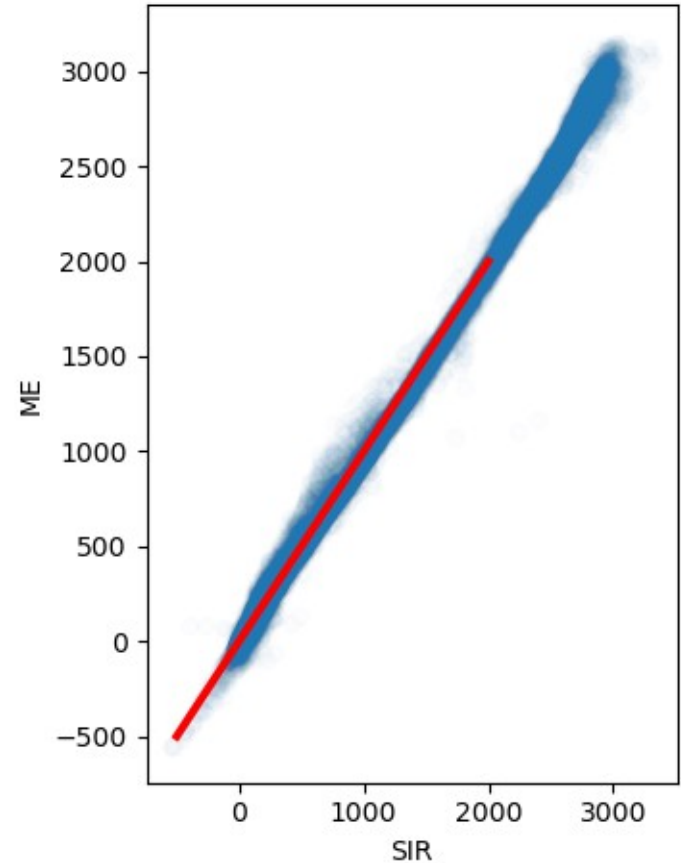
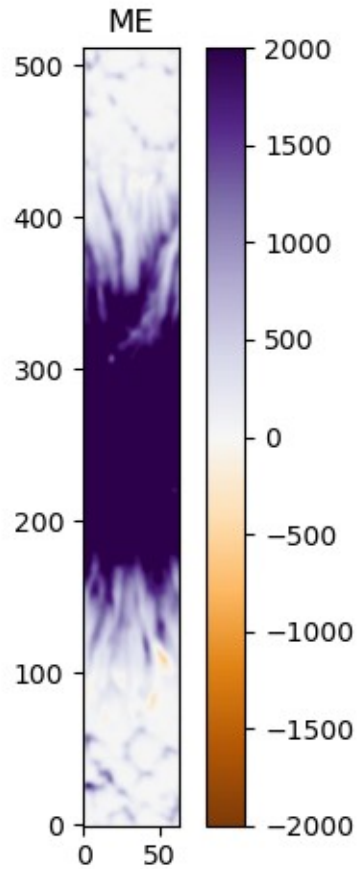
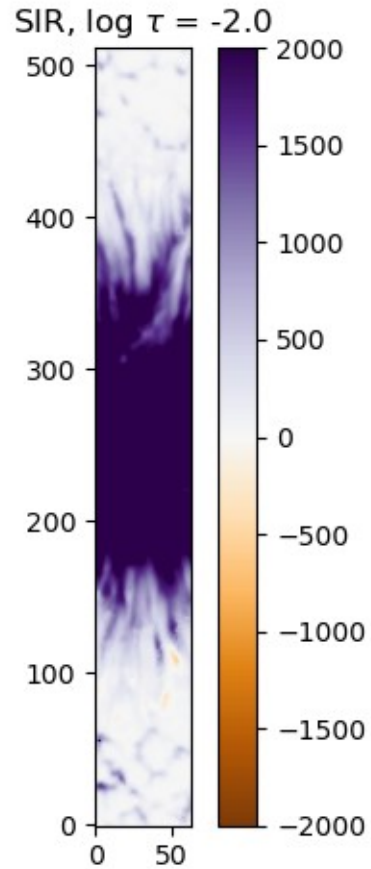


ME



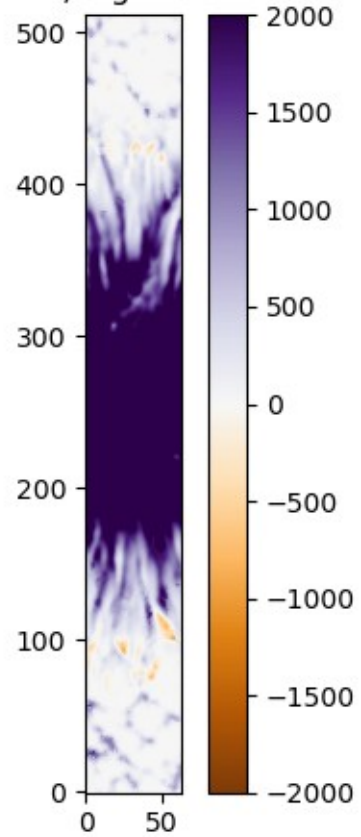


# ME vs SIR at deep photosphere

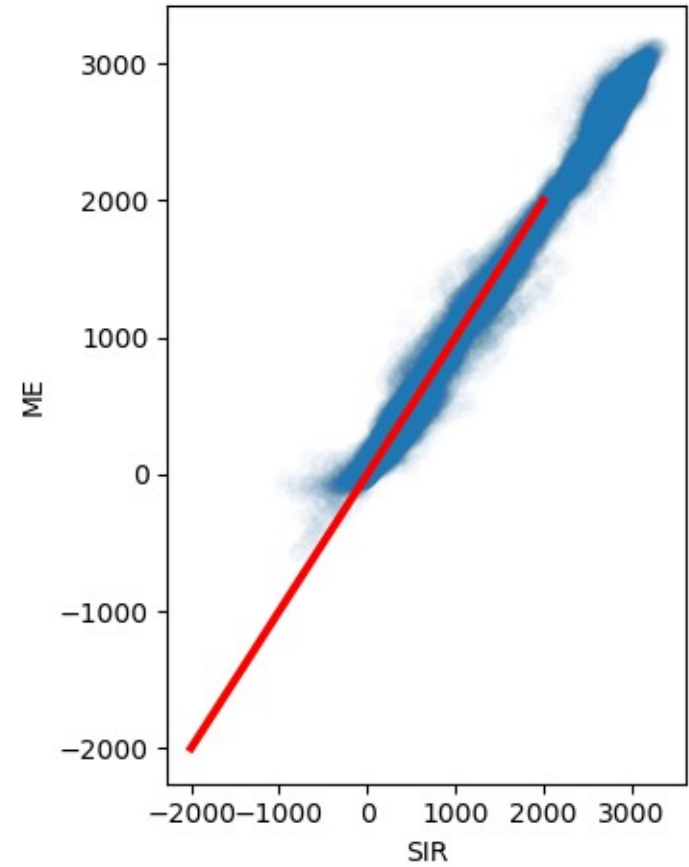
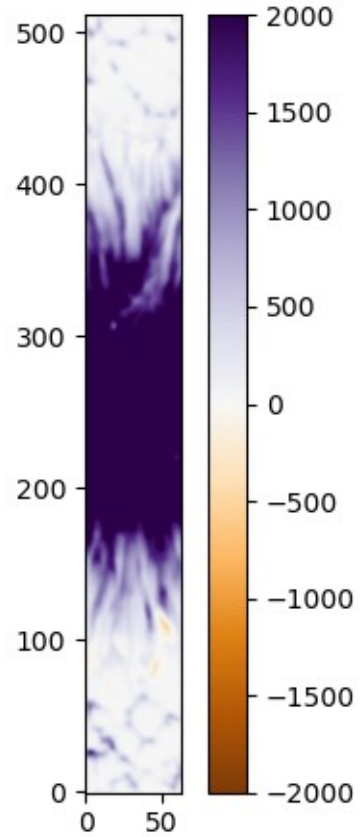


# ME vs SIR at deep photosphere

SIR,  $\log \tau = 0.0$



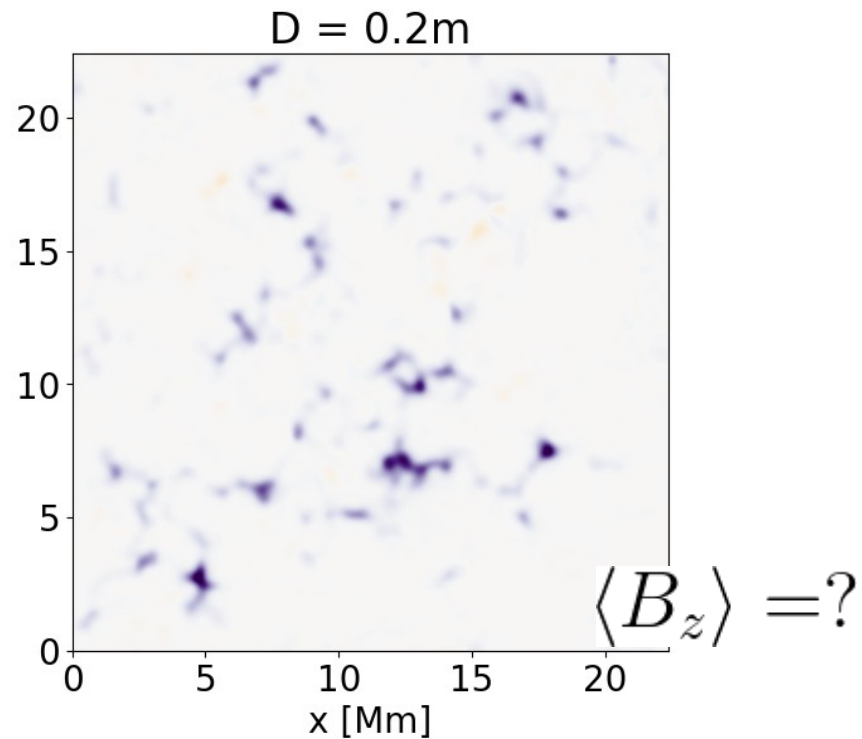
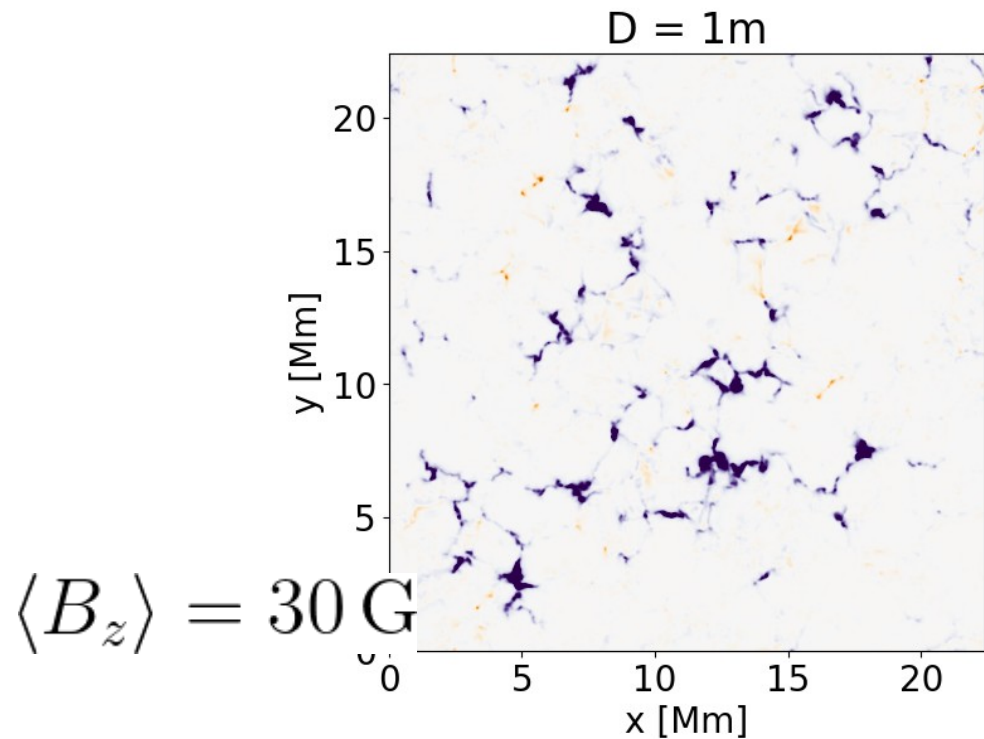
ME



# What can be done next?

- Use larger simulation, maybe with flux balance
- Apply more instrumental effects
- Apply spatially coupled inversions / apply deconvolution?
- Or just ignore and conclude that SIR is better?
- Let's have some follow up....





Difficulties in estimating photospheric magnetic fields

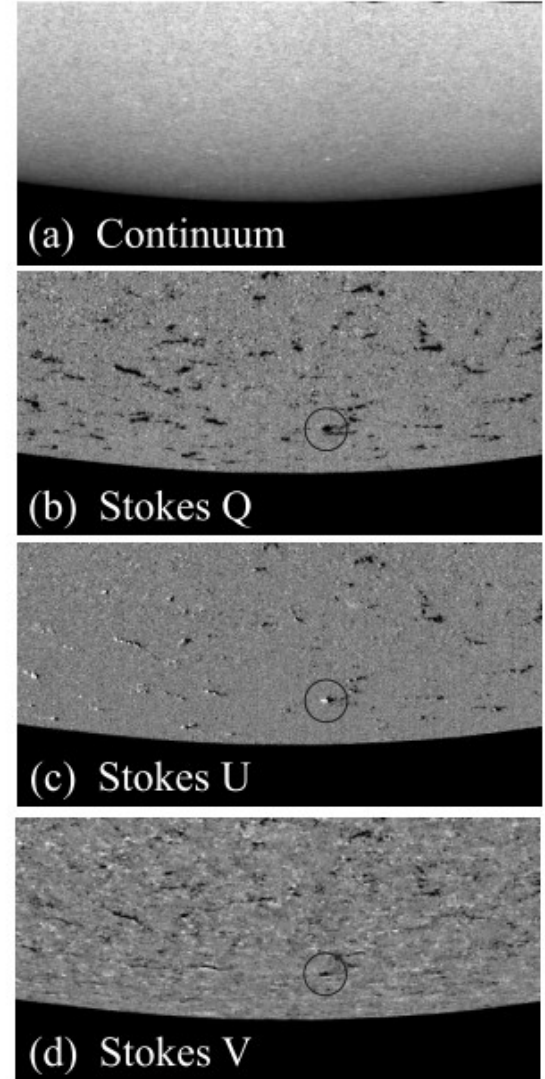
# Motivation

- Open flux especially important at the poles as it drives the solar wind – missing flux problem (Linker et al, 2017)
- Inferring polar fields is difficult
- See Tsuneta et al. (2008), Prabhu et al (2020), as well as (Ito et al 2009, Pastor Yabar et al 2018)
- To explore the limitations of inversion, we:

Model the polar observations using a MuRAM MHD cube & SIR → Invert the synthetic data using various approaches

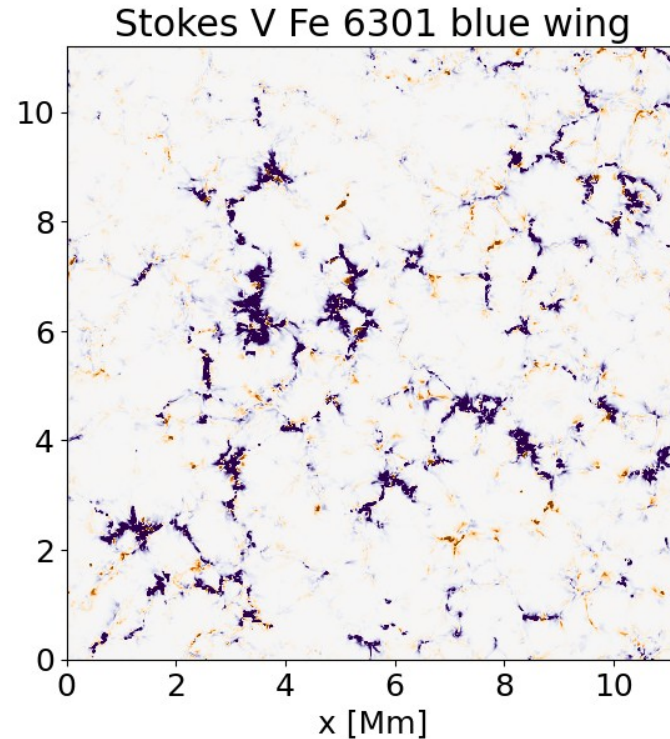
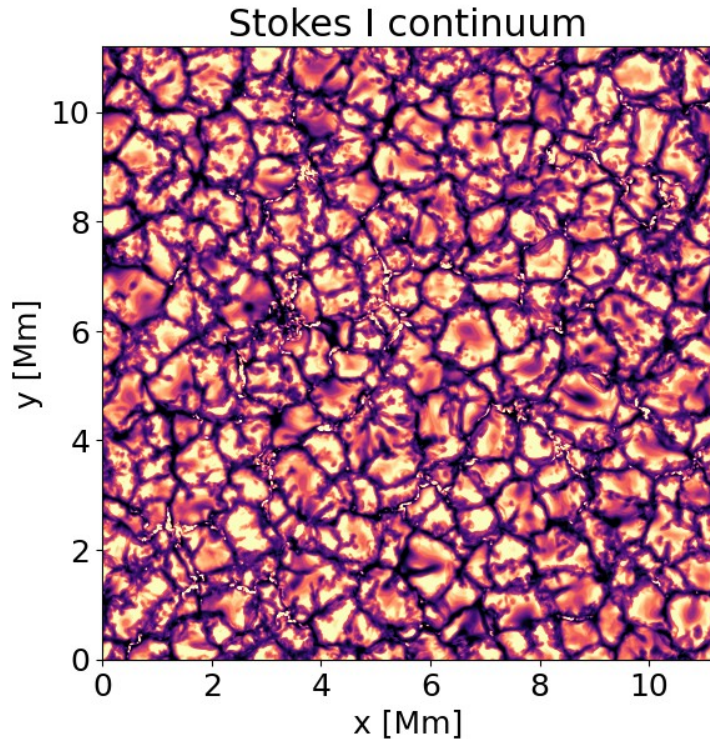
- We analyze the influence of: Spatial resolution, Viewing geometry, Inversion approach: (ME, ME + filling factor, depth stratified)

Right: Hinode SOT/SP observations from Tsuneta et al. 2008



# Setup

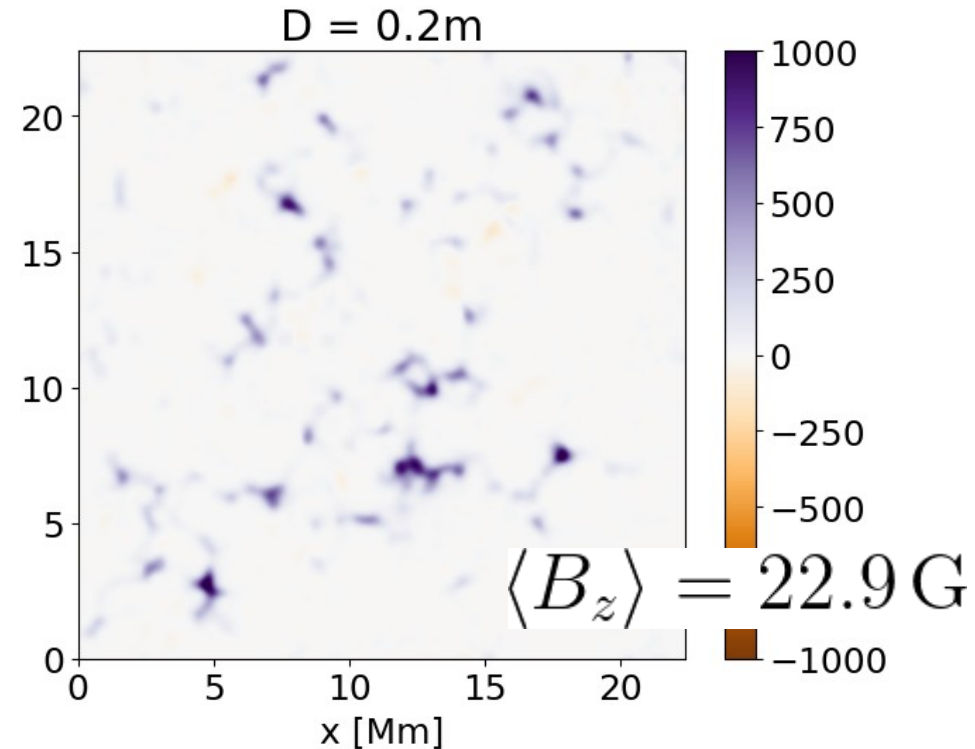
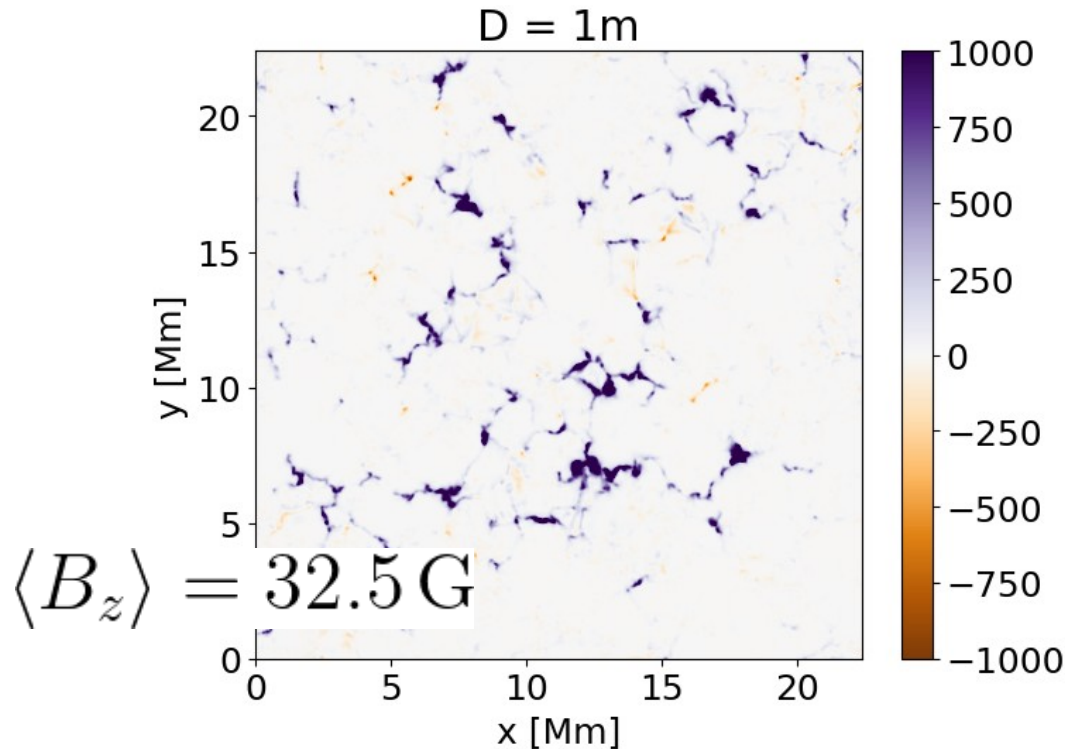
- The mean vertical field in the simulation is 30 Gauss – Ideally, we want to recover this with a given instrument and viewing geometry
- We synthesize widely used 6301/6302 lines of Fe I in LTE, at the disk center and at  $\mu = 0.4$ . At the “pole” cube is tilted, spectra synthesized and spatially binned





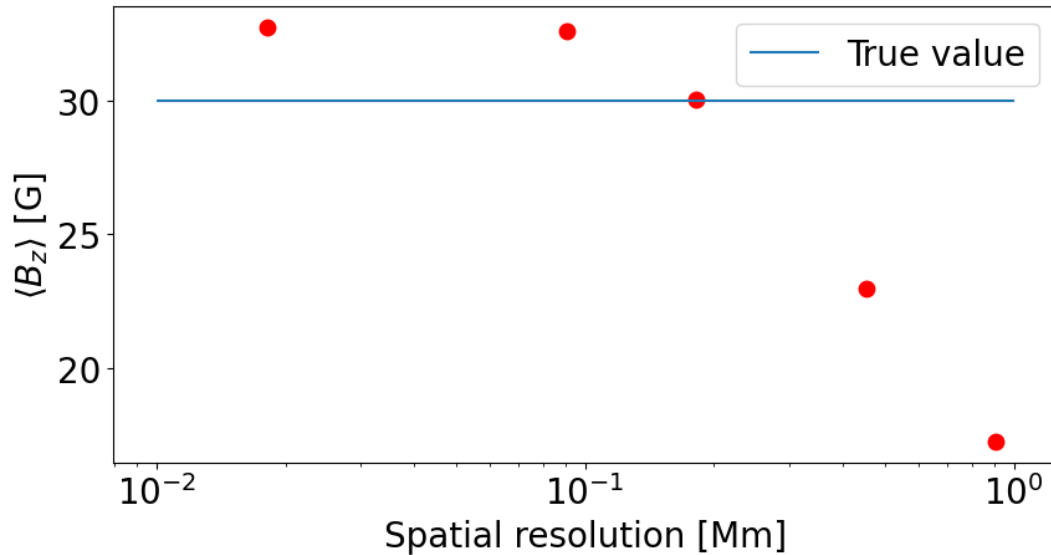
# Disk center

- The mean vertical field in the simulation is 30 Gauss – Ideally, we want to recover this with a given instrument and viewing geometry
- Sanity check: Disk center. However... (Standard Milne-Eddington inversion)

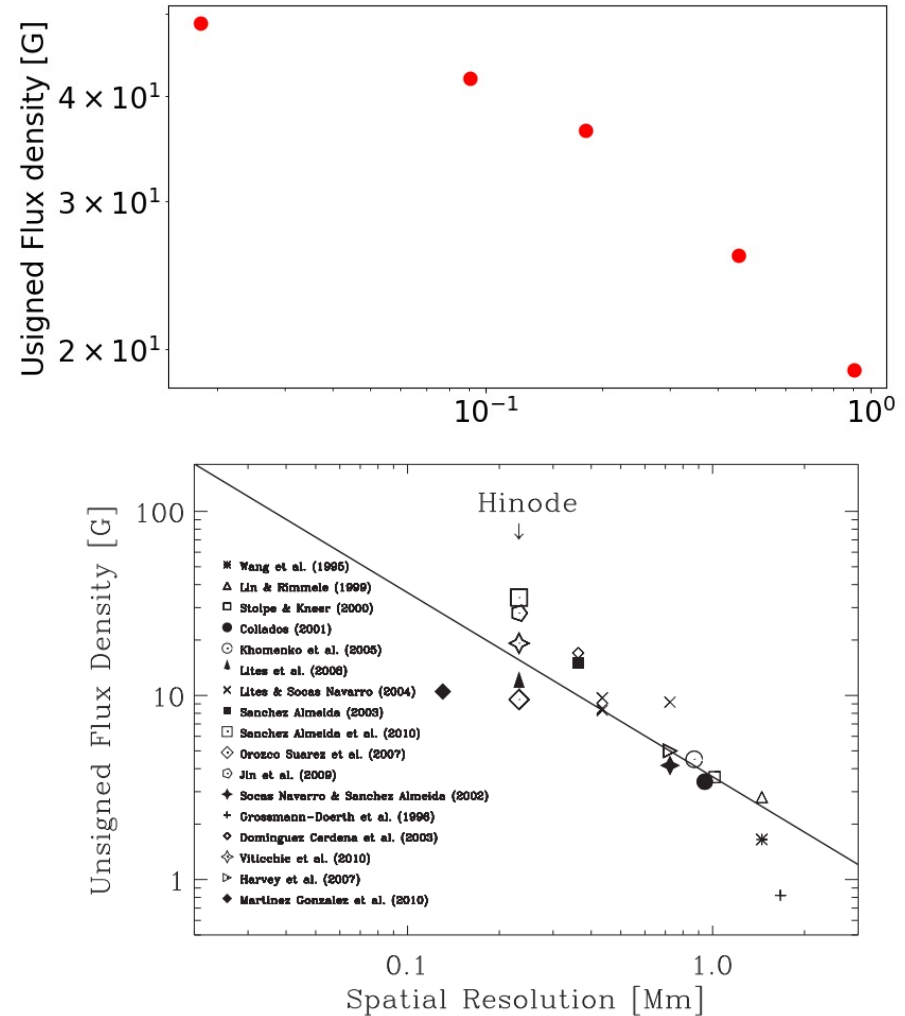


# Disk center

- Decrease in the spatial resolution  $\rightarrow$   
Decrease of both net and the unsigned flux:

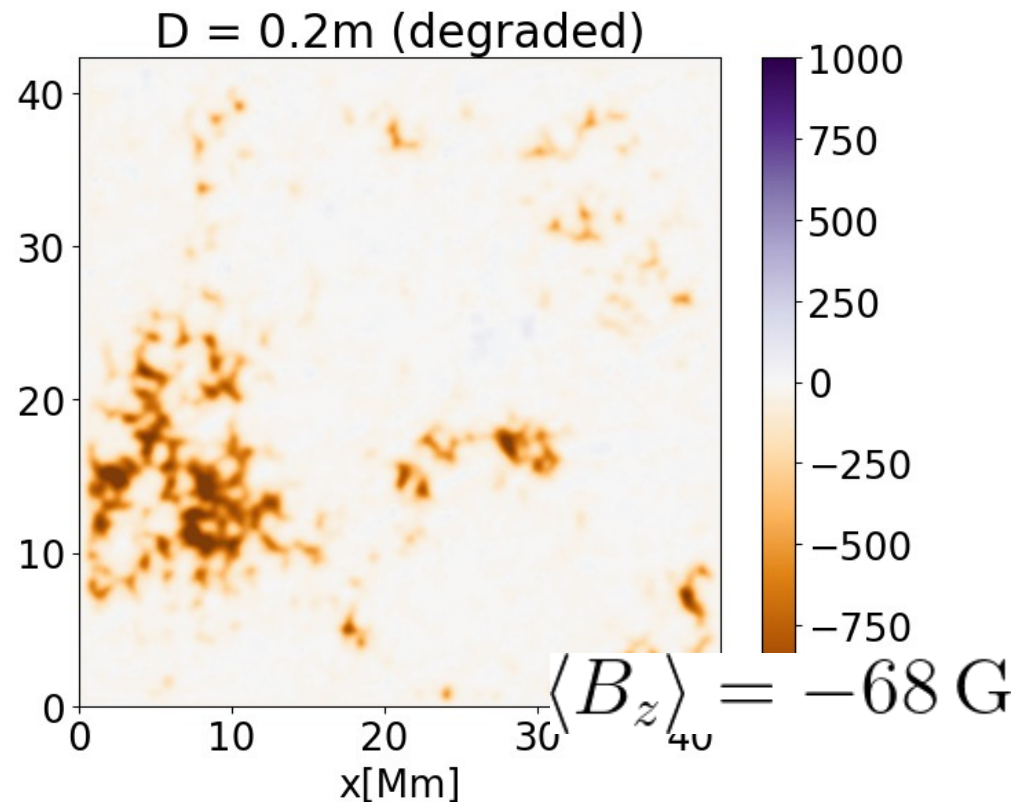
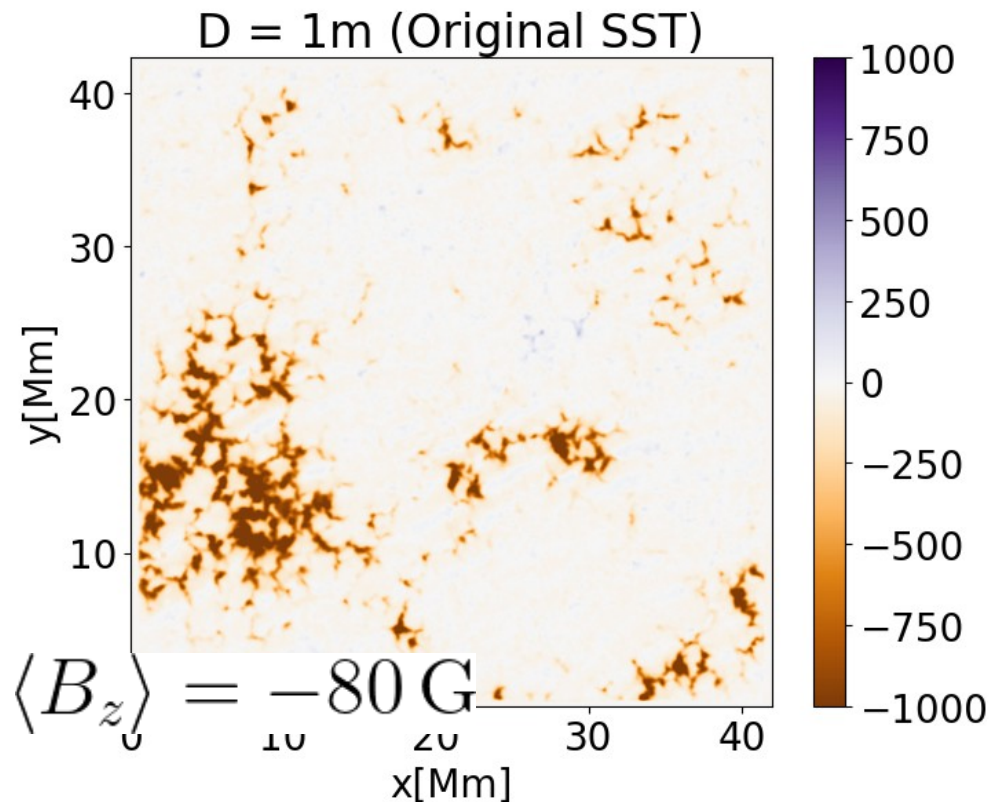


Right: Unsigned Flux density vs. Spatial resolution, from Sanchez Almeida & Martinez Gonzalez (2011)



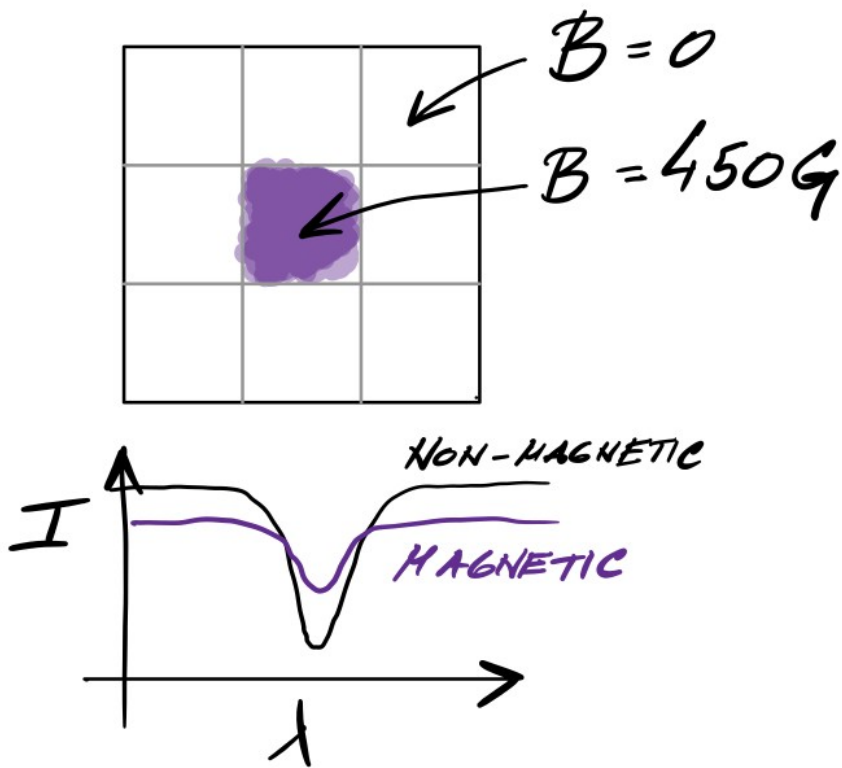
# Replication with the real data

- Fe I 630 nm lines observed @ SST/CRISP (data from Kianfar et al. 2021).



# Where does this bias come from?

- Inversion is a non-linear process. PSF application is linear (discussed in [Plowman and Berger 2020a,b,c](#), GONG end-to-end simulation)
- This effect will appear even in the weak field approximation. Consider the following:



$$V = kB \frac{dI}{d\lambda}$$

$$\left(\frac{dI}{d\lambda}\right)_{\text{mag}} = \frac{1}{2} \left(\frac{dI}{d\lambda}\right)_{\text{non-mag}} = x$$

$$\langle B \rangle_{\text{resolved}} = \frac{450\text{G}}{9} = 50\text{G}$$

$$\begin{aligned} \langle B \rangle_{\text{non-resolved}} &= \frac{V_{\text{tot}}}{k(dI/d\lambda)_{\text{tot}}} = \\ &= \frac{kBx}{k \times 17x} = 26.5\text{G} \end{aligned}$$

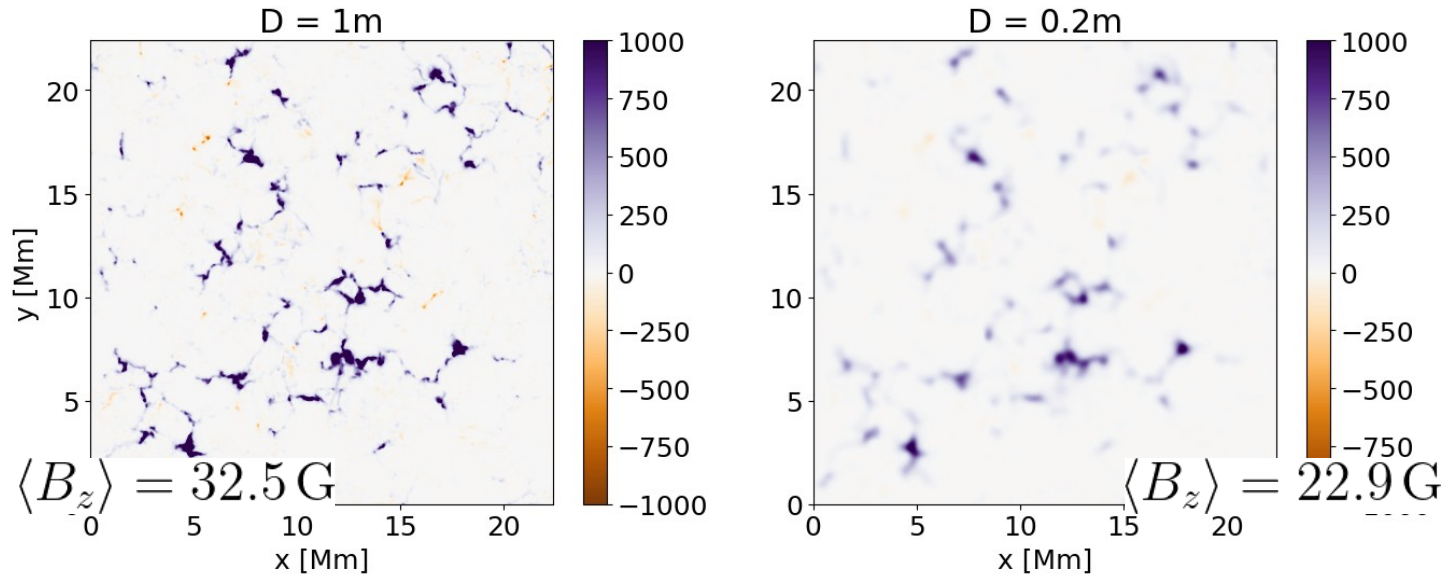
# Disk center

- This is reproduced with multiple inversion codes and PSF shapes. Repeating the experiment with simplified atmosphere we found:

At high resolutions we see more flux because of corrugation of  $\tau = 1$  surface

At low resolutions we see less flux because of RT nonlinearity

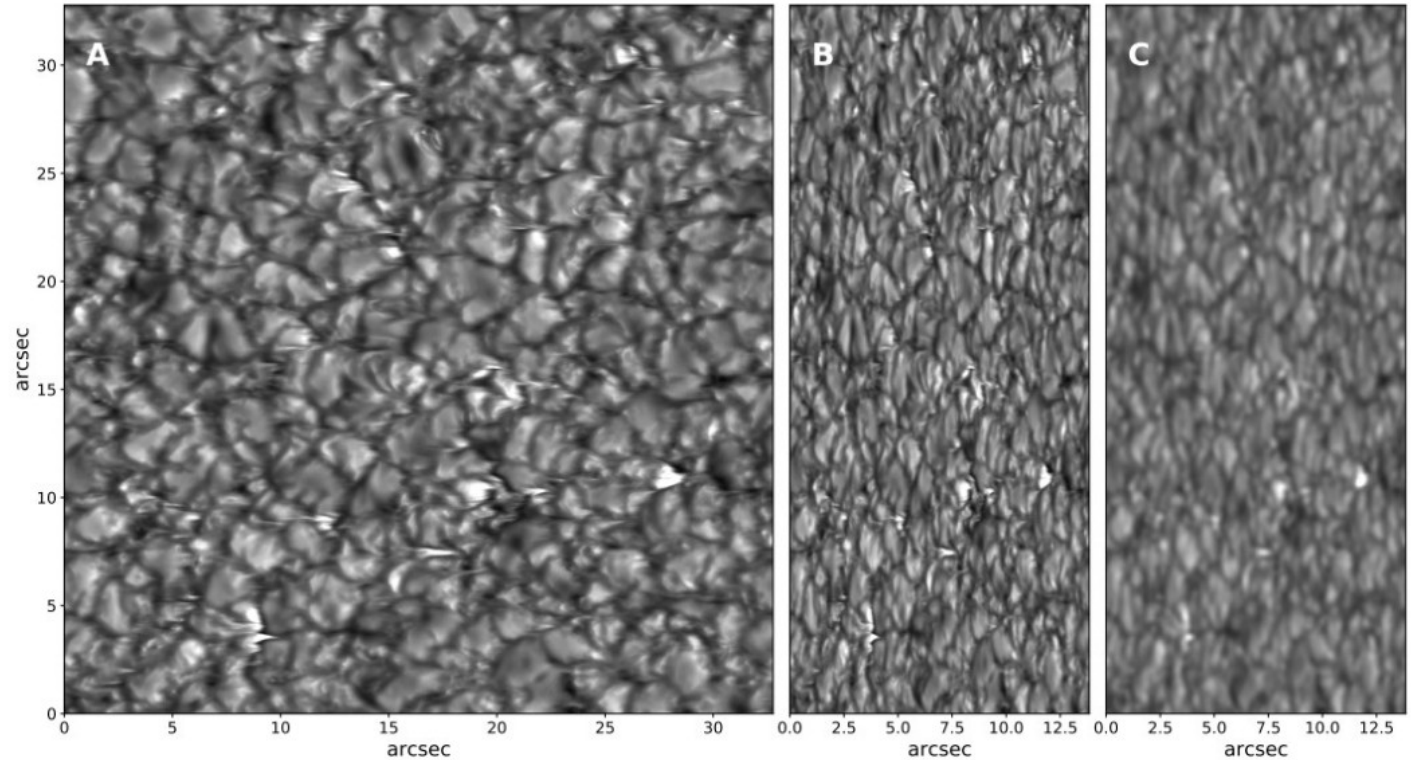
- This effect is, of course, dependent on the spatial structure of the field





# At the limb ( $\mu = 0.4$ )

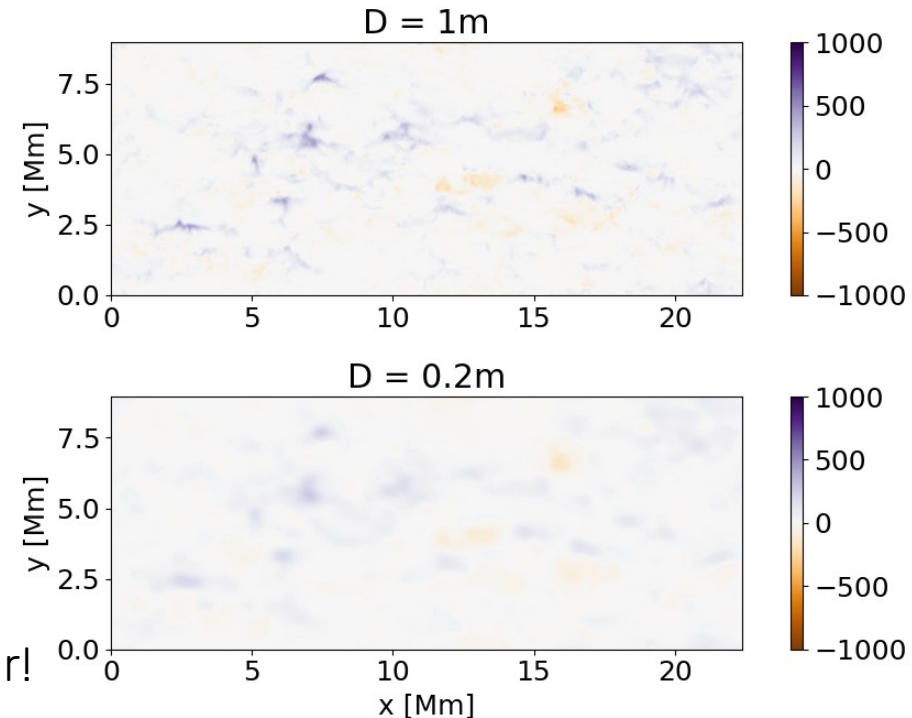
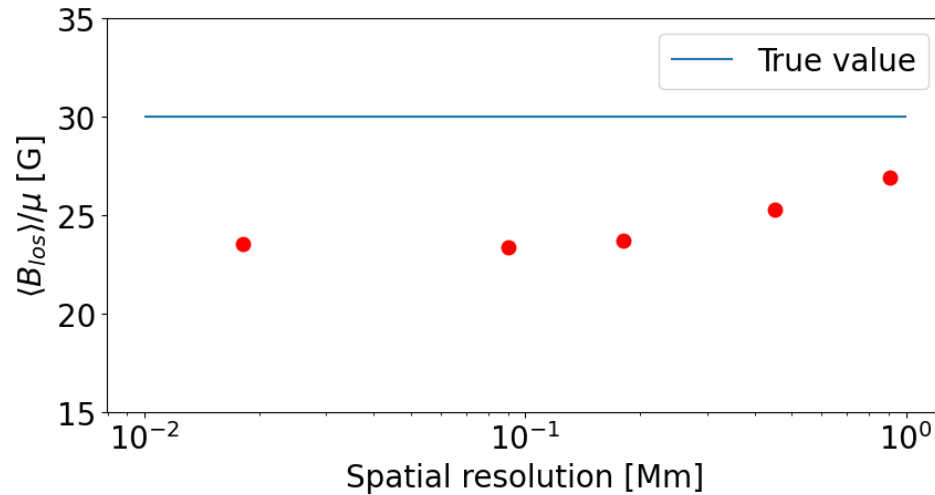
- On top of the PSF, additional effects: obliqueness + projection + noise
- Cube tilted  $\rightarrow$  Spectra are calculated  $\rightarrow$  Projected  $\rightarrow$  Application of the PSF
- Inversions with 4 different approaches: ME with local/global/no stray light, SIR (Centeno et al. 2023)



- A) Image from a tilted cube
- B) Pixels projected to LOS
- C) PSF of Hinode applied

# At the limb, the PSF effect disappears

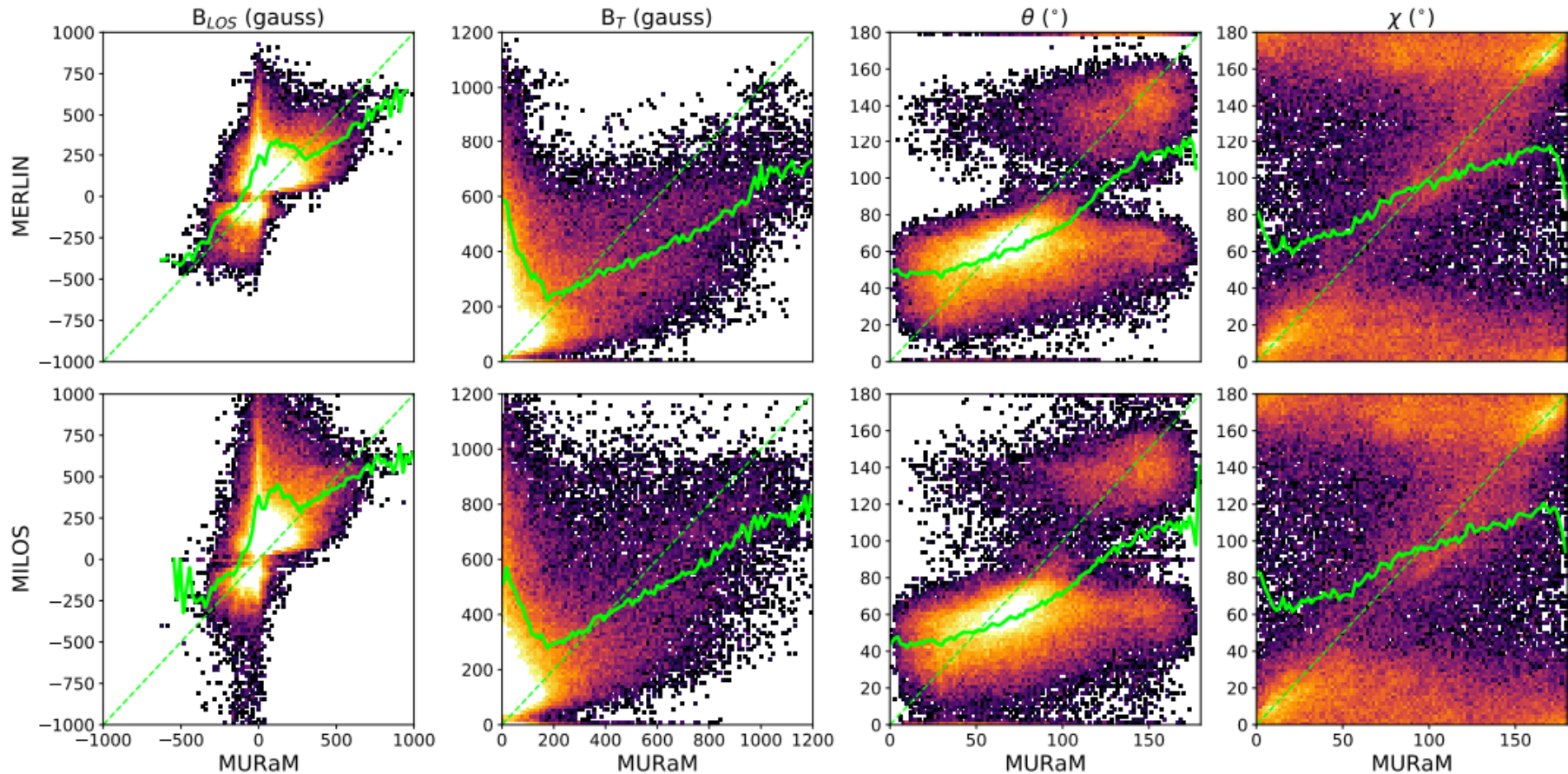
- LOS flux almost constant with the PSF – effect of decreased contrast?
- Simply de-projecting the LOS flux does not do the trick (~ 25% loss).
- Disambiguation is necessary (e.g. [Ito et al 2010](#))



- But for that we need the full magnetic field vector!

# At the limb

- (Not surprisingly), the intrinsic magnetic field properties cannot be recovered (Hinode resolution)



# Conclusions

To infer the open (net) magnetic flux, we need:

- High-resolution observations (even at the disk center) / Spatially coupled inversions
- Reliable disambiguation – *Stereoscopic methods?*
- (Maybe) multi-line / multi-height capabilities
- (Probably) good SNR
- ToDo: Extend this study with all of the above and propose observing / inversion strategies
- Questions? Comments? Suggestions?

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